

# Towards A Novel Control Framework for Robots Continuous Interactions with Environments

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# Context

Control continuity is of primary concern when robots interact with unstructured environments.

Discrete events on constraints:

- Appearance
- Disappearance
- Discontinuous variations

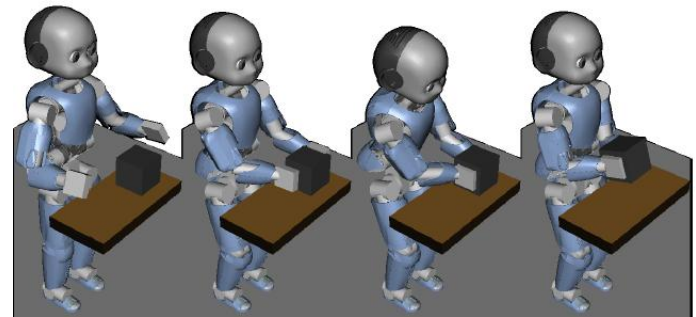


Discrete changes in the model's structure



Results of discontinuities:

- Discontinuous torques input
- Physical damages to the robot
- Lose balance, ...



**Robots should react or anticipate promptly to alleviate these discontinuities**

# Outline

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- Context
- State of the art
- Problem statement
- Current work
- Future work

# State of the art: Focus on contact constraints

## Pre-contact Phase

Avoid contacts { Current environment geometry [Ebert2002]  
Motion planning techniques [Makarov2011]

Regulate impact force { Design a light weight robot  
Reduce contact velocity  
Minimize apparent inertia

[Walker1990]

$$F_{impact} = \frac{-(1 + e)(v_1 - v_2)^T n}{n^T M_{\Xi} n}$$

## Contact Phase (if inevitable)

- Introducing passive compliance in the system [Pagilla2001]
- Adapting active compliance (control gain adaptation) [Tonietti2005]

## Post-contact Phase:

- Detect the contact occurrence [Haddadin 2008]
- Switch to an appropriate reaction strategy [Alessandro2005]
- Perform complex tasks with the environment

# Control Framework

Dynamic Model

$$M(q)\ddot{q} + n(q, \dot{q}) = J_c^T \chi$$

Jacobian matrix of contact point

$$J_c^T = [J_{con}^T \quad S^T]$$

Tasks Definition

$$\ddot{x}_i = J_i \ddot{q} + \dot{J}_i \dot{q}$$

Selection matrix of actuated DOF

Constraints

$$A\chi = b \quad G\chi \leq h$$

$\chi = [w_c^T \quad \tau^T]^T$  : Action variable

LQP Formulation (Weighting Strategy) [Salini2012]

$f_i$  : Different tasks

$w_i$  : Weight gain

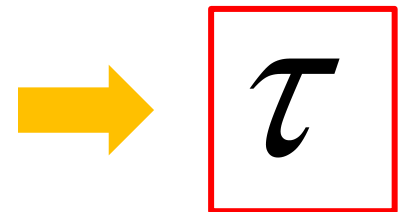
$$\min_{\chi} \quad \frac{1}{2} (\sum_i (w_i f_i(\chi))^2 + (w_0 f_0)^2)$$

$$\text{s.t.} \quad J_c^T \chi = M\ddot{q} + n$$

$$f_i(\ddot{q}, \ddot{x}^d) = J_i \ddot{q} + \dot{J}_i \dot{q} - \ddot{x}_i^d$$

$$A\chi = b$$

$$G\chi \leq h$$



Control torques

# Problem and objective

## Control in free space

Model:  $M(q)\ddot{q} + n(q, \dot{q}) = S\tau$

$$|q| \leq q_{\max}$$

Actuation constraints:

$$|\dot{q}| \leq \dot{q}_{\max}$$

$$|\tau| \leq \tau_{\max}$$

Force constraints:

NULL

## Control in contact

Model:  $M(q)\ddot{q} + n(q, \dot{q}) = S\tau + J^T W_{con}$

$$|q| \leq q_{\max}$$

$$|\dot{q}| \leq \dot{q}_{\max}$$

$$|\tau| \leq \tau_{\max}$$

$$W_{con} \geq 0 \Rightarrow W_{con} \leq \begin{cases} W_1 & t \leq t_a \\ W_2 & t > t_a \end{cases}$$

$$J_c \ddot{q} + \dot{J}_c \dot{q} = 0$$

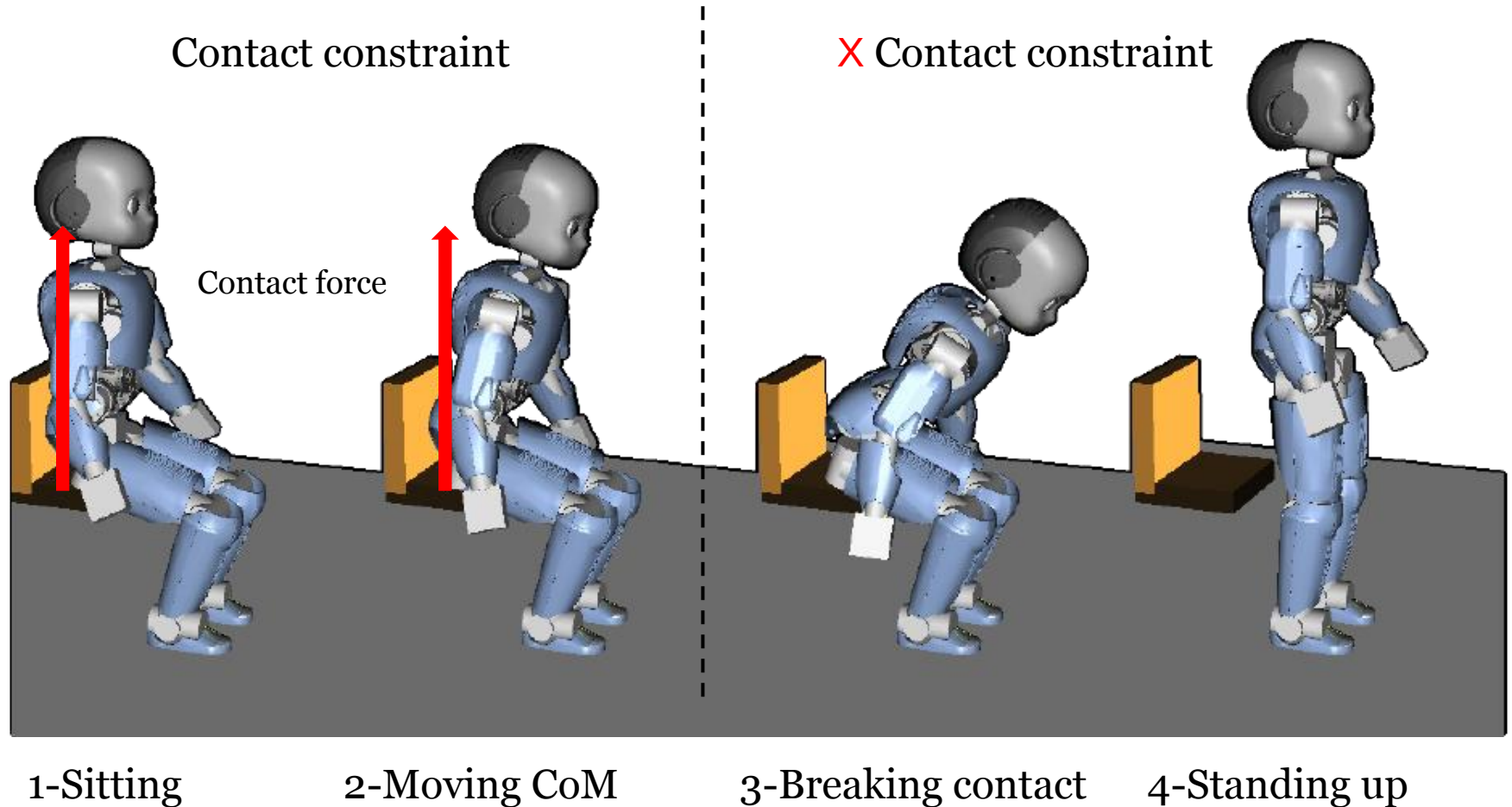
Discontinuous events

## Objective

Continuous control torque to guarantee robot's performances under discontinuities

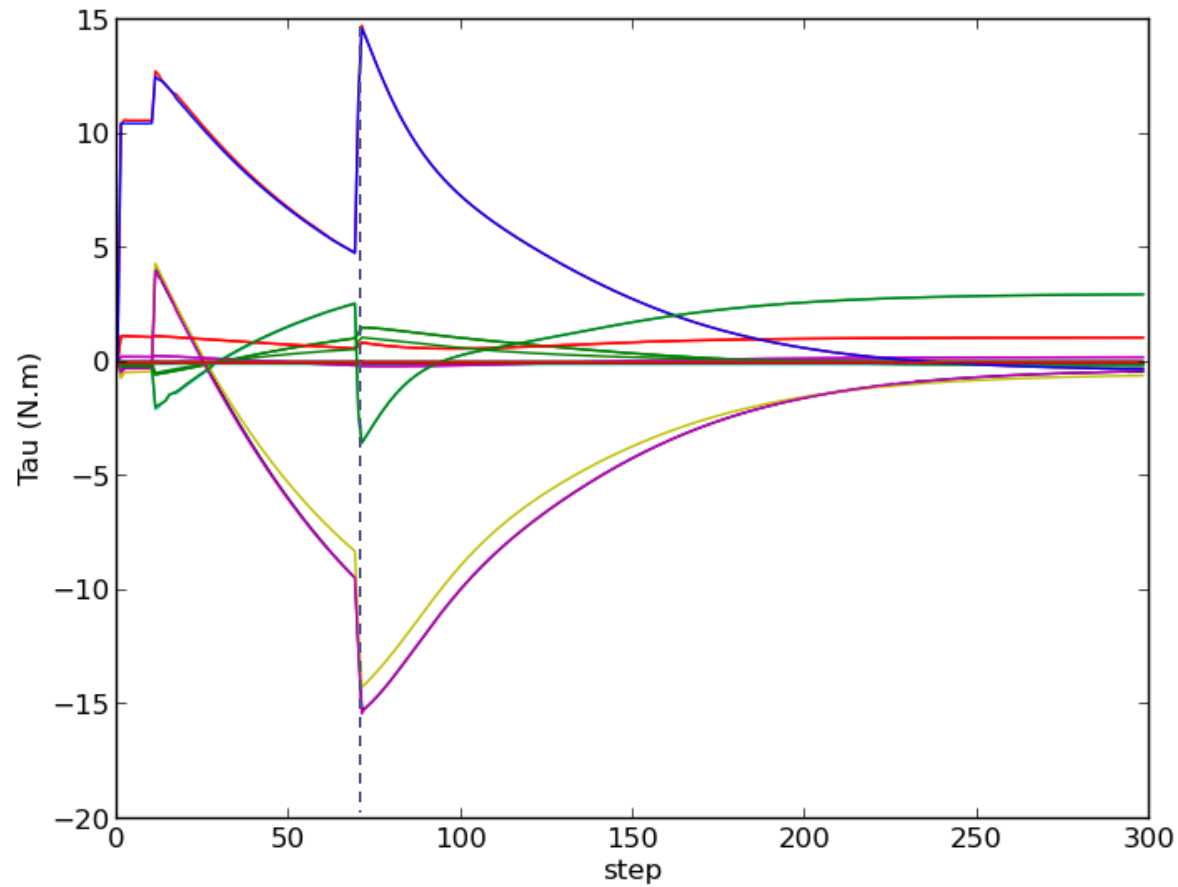
# Current work

## Constraints Disappearance



# Current work

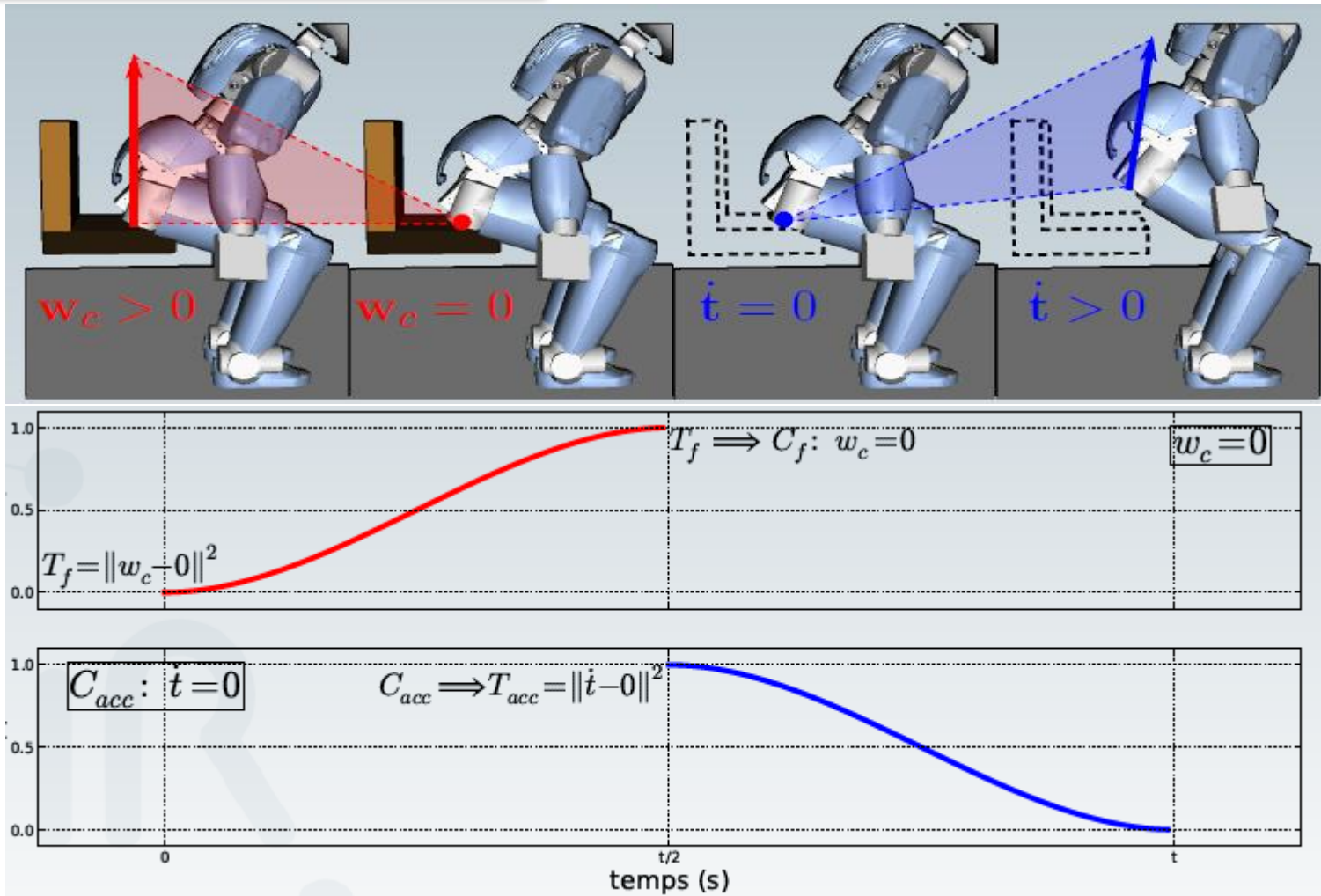
## Results



Evolution of control torques

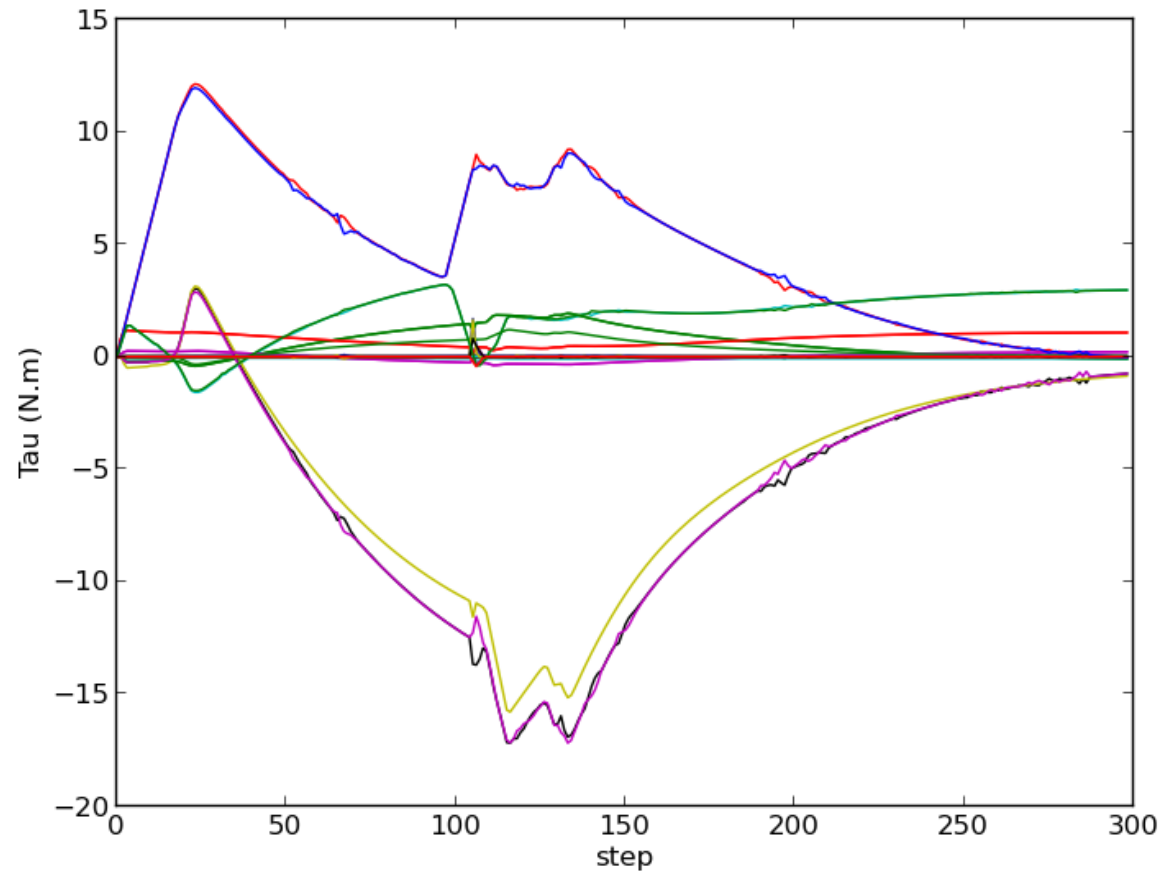
# Current work

## Constraint transition strategy



# Current work

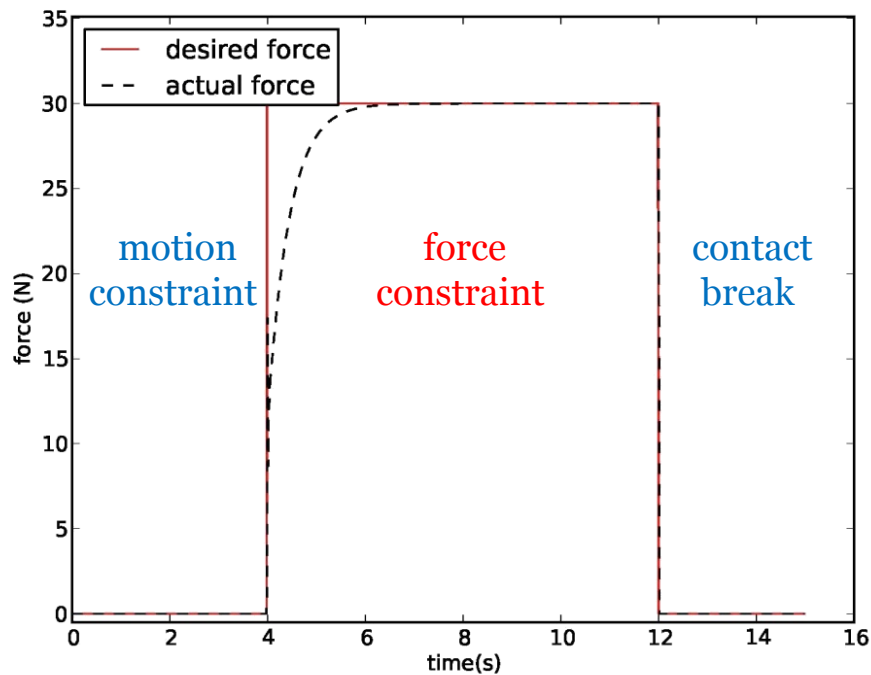
## Results



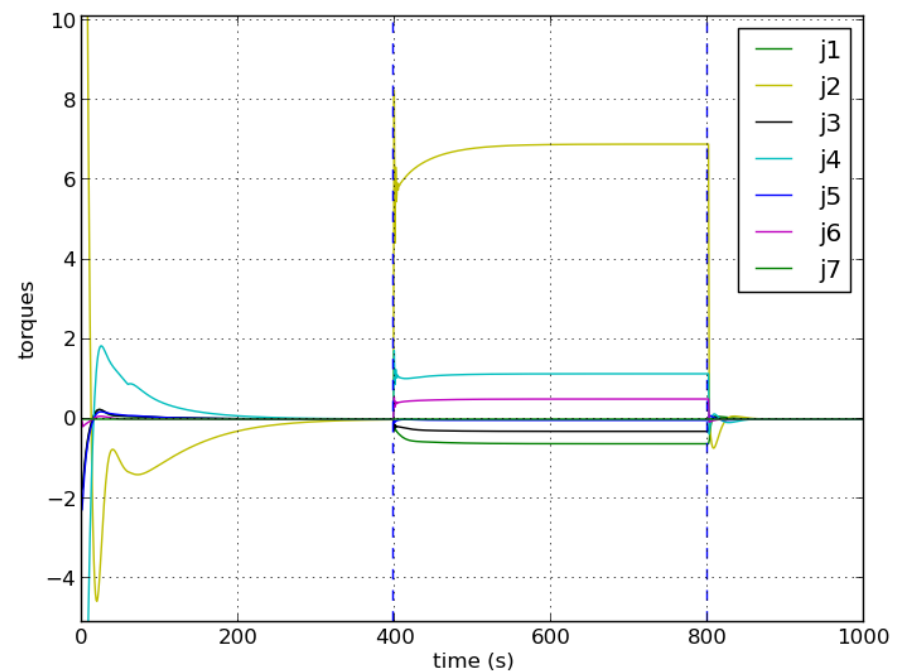
Evolution of control torques

# Current work

Switches between motion constraint and force constraint



Reference force and actual force



Control torques

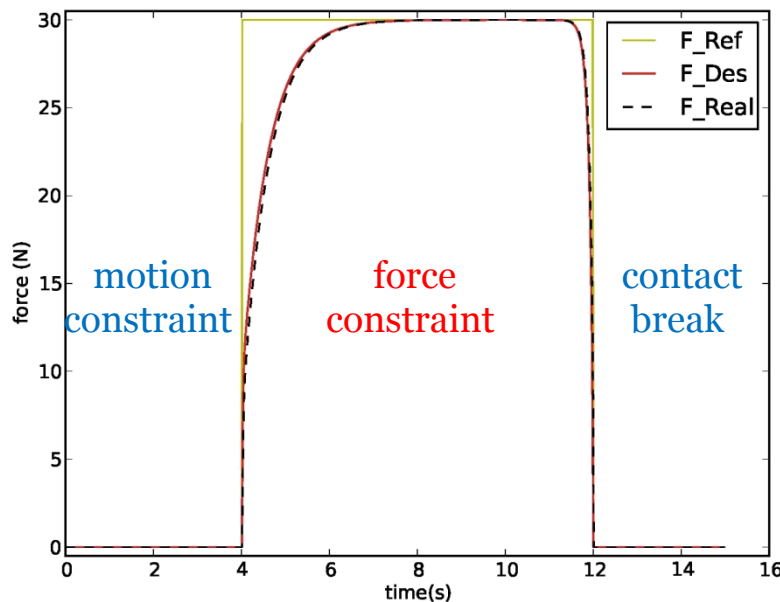
# Current work

## Proposed strategy with MPC

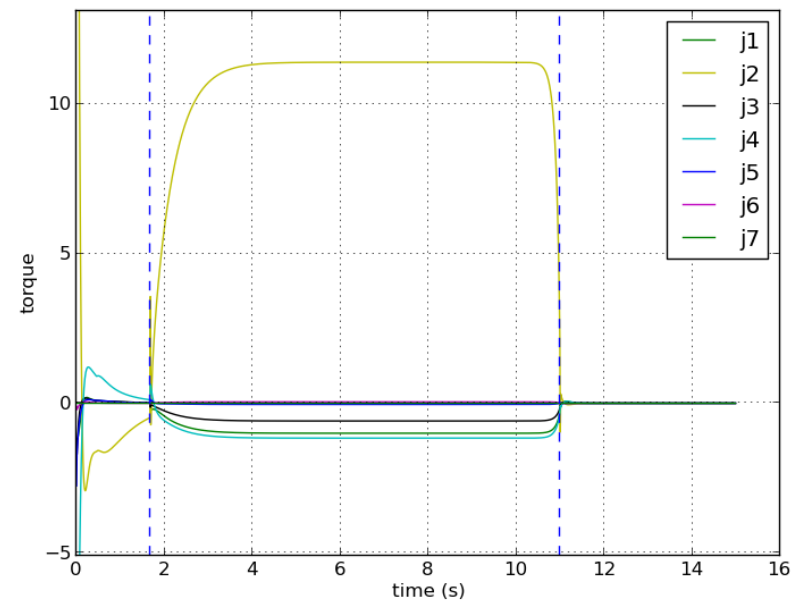
Force control model:  $F(t+1) = AF(t) + Bu(t)$   
 $A=1 \quad B=1$

$F(t)$  : Force state vector  
 $u(t)$  : Force Control input  
 $P, Q, R$  : Gains

Cost function:  
 (Horizon  $N$ )  $J := \min_U \frac{1}{2} F_N^T P F_N + \frac{1}{2} \sum_{k=0}^{N-1} (F_k^T Q F_k + u_k^T R u_k)$



Reference force and actual force



Control torques

## Future work

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1. Intelligent constraint transition strategy
2. MPC can deal with whole dynamics of robots
3. General control framework combines both 1 and 2
4. Verify this control framework on real iCub robot

Thank you